

Inference at * 1
of proof for Lemma adjacent-before:

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1.  $T : \text{Type}$ 
2.  $L : T \text{ List}$ 
3.  $x : T$ 
4.  $y : T$ 
5.  $i : \{0..(\|L\| - 1)^-\}$ 
6.  $x = L[i]$ 
7.  $y = L[(i+1)]$ 
 $\vdash \exists f : \{0..2^-\} \rightarrow \{0..\|L\|^-\}. (\text{increasing}(f;2) \ \& \ (\forall j : \{0..2^-\}. [x; y][j] = L[(f(j))]))$ 
  by (((InstConcl [ $\lambda j.$ if ( $j =_0 0$ ) then  $i$  else  $i+1$  fi ]))
    CollapseTHEN (Auto'))·)

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  CollapseTHEN (((RepUR “increasing“ ( 0)·)
CollapseTHEN (MaAuto·))·)·

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1:

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8.  $i@_0 : \{0..1^-\}$ 
 $\vdash \text{if } (i@_0 =_0 0) \text{ then } i \text{ else } i+1 \text{ fi} < \text{if } (i@_0+1 =_0 0) \text{ then } i \text{ else } i+1 \text{ fi}$ 

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2:

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8.  $\forall i@_0 : \{0..1^-\}. \text{if } (i@_0 =_0 0) \text{ then } i \text{ else } i+1 \text{ fi} < \text{if } (i@_0+1 =_0 0) \text{ then } i \text{ else } i+1 \text{ fi}$ 
9.  $j : \{0..2^-\}$ 
 $\vdash [x; y][j] = L[\text{if } (j =_0 0) \text{ then } i \text{ else } i+1 \text{ fi}]$ 
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